

Allan Kaufman on behalf of the CAS RBC Dependencies and Calibration Working Party

Introduction

- Dependencies and Calibration Working Party (DCWP) of the CAS

 Researching methods for calibrating P&C RBC parameters
 - Particularly underwriting and reinsurance risks
 - Many workstreams, many contributors (see appendix)
- Caveats
 - The analysis is solely the responsibility of the work stream participants, DCWP members and not that of their employers, the CAS or the American Academy of Actuaries
 - Presentation assumes the audience has a working knowledge of Standard Formulas
 - Some slides describe preliminary work, which may change materially as research progresses
- Results published in CAS E-Forum when finalized

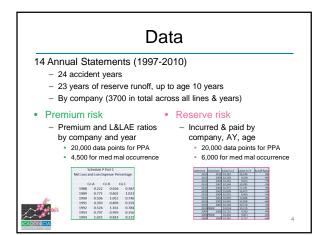
Key Findings

- 1. Size (LOB-size) matters
 Not surprising... but it's not just "law of large numbers"

 2. Type of company
 Especially significant for specialty
- 2. Type of company matters
- 3. Diversification Little difference between simple and complex metrics

lines

- 4. Diversification effect
- 5. Time scale matters
- Bottom up (100+ parameters) vs. top down (2 parameters) Need enough years of data to work with





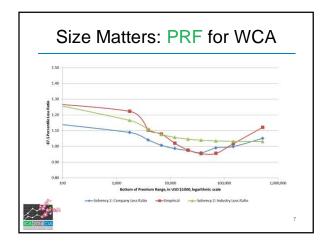
RBC Formula: UW Risk Charges Factors applied to premium or reserves by LOB

- Premium Risk Factors (PRFs)
- Reserve Risk Factors (RRFs)
- Selected factors are adjusted for
 - Investment income
 - Own-company experience
 Loss sensitive contracts
 - (For PRFs) own-company expenses.
- Indicated factors: 87.5th percentile observed from all companies (after filtering) by LOB
 - Due to size effects, actual average safety margin is 90th-95th percentile
- Diversification reflected through "70% rule"

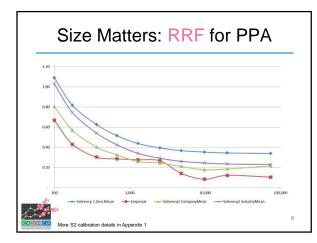
1. Size Matters

- Indicated risk charge (87.5th percentile) varies with size
- Pattern appears to depend on factors in addition to size
- Standard formulas generally choose risk charge that does not vary with size, e.g.

- Median
- Based on "large enough" companies









2. Type of Company Matters

- Risk charge varies by type of company

 Reinsurer, standard lines insurer, PL specialist, etc.
- Calibrating on data points that exclude "minor lines" removes much (but not all) of the effect
 - "Minor line" = LOB as % of total company less than some threshold (e.g., 5%)



Exhibit 3.1: PRFs - A	II Reinsurers		vs. Non-Rein nce before m	surer inor line filter			
		(1)	(2)	(3)	(4)	(5)	(6)
		Incl	uding Minor L	ines	Exc	luding Minor	Lines
Line of Business (LOB	9	Specialists	Non- Specialists	Difference	Specialists	Non- Specialists	Difference
A	Homeowners/Farmowners	0.908	0.966	-0.057	0.874	0.956	-0.082
В	Priv. Passenger Auto Liability	1.079	0.982	0.097	0.998	0.973	0.025
с	Commercial Auto Liability	1.122	0.984	0.139	0.979	0.982	-0.003
D	Workers' Compensation	1.202	1.053	0.149	1.067	1.04	0.027
E	Commercial Multiperil	1.041	0.922	0.118	1.002	0.881	0.122
F1	Medical Mal Occurrence	1.599	1.667	-0.068	N/A	1.458	N/A
F2	Medical Mal - Claims made	1.308	1.2	0.108	0.946*	1.147*	(0.201)*
н	Other Liability	1.194	1.011	0.183	1.07	1.016	0.053
1	Auto Physical Damage	0.925	0.862	0.064	0.806	0.842	-0.036
N&P	Reinsurance A & C	1.331	1.621	-0.291	1.288	1.303	-0.015
0	Reinsurance B	1.329	1.652	-0.323	1.306	1.343	-0.037

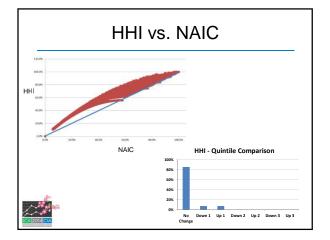
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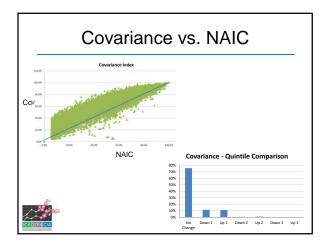
3. Diversification Metrics NAIC RBC diversification measure (Max LOB Premium)/(All LOB premium)

- Alternative diversification measures
 HHI index (sum of squares of percentages by LOB)
 Covariance matrix
- Company diversification rankings similar, *regardless* of diversification measure

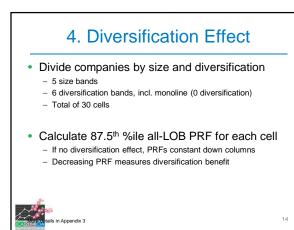


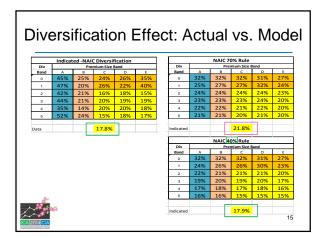












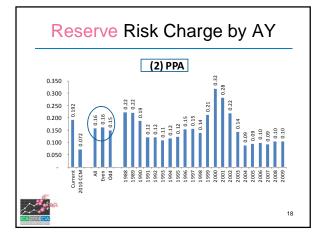


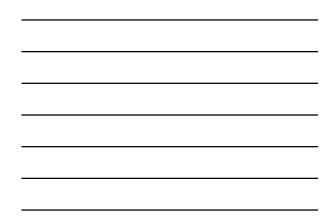
5. Time Scale Matters

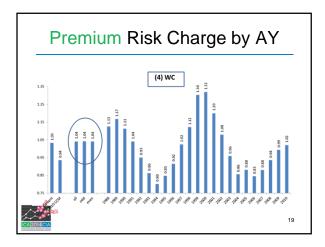
- PRF and RRF by AY show UW cycle effects
- Even/Odd test over 24 AYs appears reasonably stable
 - Also tested every 4^{th} year for stability

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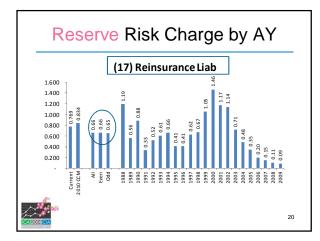










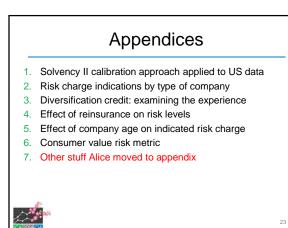


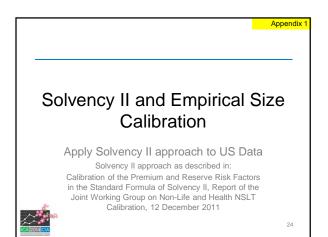


(Too much for	Other Findings discussion today; See appendices)
Consideration	Finding
6. Reinsurance-related risks	Reinsurance risk is not just counterparty solvency risk
7. Age of company	Companies with more years of experience appear to have lower risk charges
8. Arbitrary safety metric	"Consumer Welfare" metric is an alternative
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Solvency II Loss Ratio Model

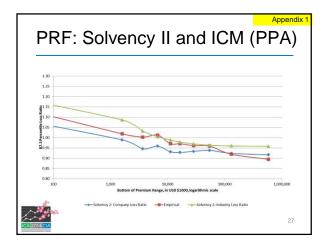
Appendix 1

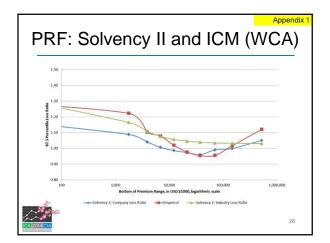
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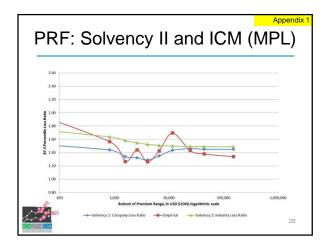
- · Random loss ratios driven by compound poison process
- Variance related to size (premium)
- Parameters vary over time
- The expected value of the random process is the expected loss ratio
- The variance of the process is a quadratic function of size and size-squared
 - Linear size-term implies variance goes to zero
 - Quadratic size-term implies variance goes to constant value
- Error function normal or lognormal — Normal illustrated here

- Appendix Solvency II Loss Ratio Model
- Loss ratio and variance parameters can be industry-wide values or company specific values
 - Data sparser for company-specific parameters, but fit better
 - We consider both industry and company loss ratio parameters
 - Use only industry variability parameter
- Normal and Lognormal error functions produce similar results
 - Neither is a very good fit to small or large LOB-sizes



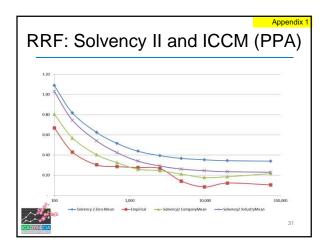




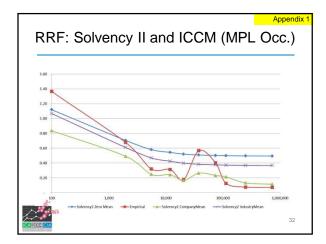




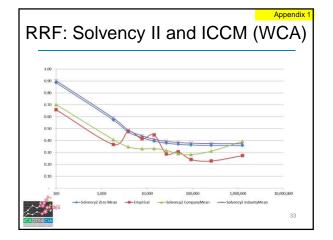
- Same model
- Size = initial reserve
- Comments regarding premium apply equally to reserve runoff
- Consider expected runoff =
 - Industry average,
 - Company specific, or
 - Zero



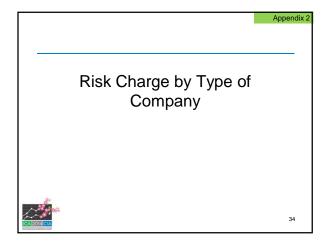


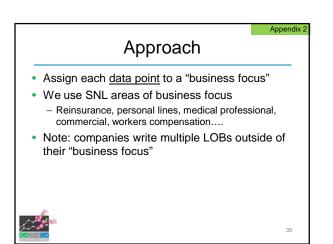












Approach

- Use ICM baseline database to determine 87.5th percentile loss ratio (PRF)
 - By LOB
 - Separately for companies within each "business focus"
- Data considerations
 - Pools assigned business focus based on majority of number of companies in DCWP -defined pool
 - Business focus based on current mix of business; historic mix (24 years) may be different

Appendix 2

Findings

Appendix 2

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- "Minor line" filter mitigates differences by type of company
 - PRF differences by type of company smaller after minor line filter
 - Type of company differences remain

Observations: Appendix Business Focus = Reinsurance

- We'll refer to Reinsurers as "specialists"
- Specialist PRFs are lower than non-specialist PRFs in specializing lines [Lines N&P and O]; [Next slide: [Are Col 3 & 6 <0]
- Difference between specialists and non specialists is smaller with minor line filter than without minor line filter. [Is |Col 6| < |Col 3|?]
- For non-specializing LOBs, Specialist PRFs are not always higher or lower than non-Specialist PRFs. [Col 6 > or < 0]

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с	Commercial Auto Liability	1.122	0.984	0.139	0.979	0.982	-0.003
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0	Reinsurance B	1.329	1.652	-0.323	1.306	1.343	-0.037



Appendix 2 Observations: Business Focus = Personal Lines

- We'll refer to Personal Lines Companies as "specialists"
- Specialist PRFs are lower than non-specialist PRFs in specializing lines [Lines A & B]; [Are Col 3 & 6 <0]
- Difference between specialists and non specialists is (slightly) smaller with minor line filter than without minor line filter. [Is |Col 6| < |Col 3|?]
- For non-specializing LOBs, Specialist PRFs are lower than non-Specialist PRFs. [Col 6 > or < 0]

Exhibit 3.2: PRFs - F		i com	(1748-1	20100	10.2	weat	1000
Exhibit 3.2: PRFs - F	ersonal Lines	(1)	(2)	(3)	(4)	(5)	(6)
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Line of Business (LOB	9	Specialists	Non- Specialists	Difference	Specialists	Non- Specialists	Difference
A	Homeowners/Farmowners	0.954	0.981	-0.027	0.952	0.958	-0.006
в	Priv. Passenger Auto Liability	0.949	1.045	-0.096	0.947	1.028	-0.08
с	Commercial Auto Liability	0.9	1.023	-0.122	0.904	0.998	-0.095
D	Workers' Compensation	0.965	1.085	-0.121	0.944	1.06	-0.116
E	Commercial Multiperil	0.857	0.965	-0.108	0.814	0.917	-0.104
G	Special Liability	0.931	1.014	-0.083	1.201	0.943	0.258
н	Other Liability	0.902	1.054	-0.151	0.865	1.033	-0.168
1	Auto Physical Damage	0.846	0.884	-0.038	0.844	0.839	0.005
N&P	Reinsurance A & C	1.553	1.523	0.031	1.2	1.302	-0.102
				\bigcirc			

Observations:

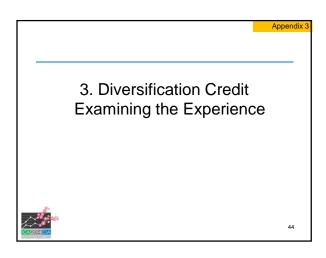
Business Focus = Commercial Lines

- We'll refer to Commercial Lines Companies as "specialists"
 Commercial Lines is all lines except Personal and Reinsurance
- Specialist PRFs are not generally lower than non-specialist PRFs in specializing lines [All lines excl. A, B & O]; [Are Col 3 & 6 <0]
- Difference between specialists and non specialists is not particularly smaller with minor line filter than without minor line filter. [Is |Col 6| < |Col 3|?]
- It may be that this category is too diverse to reflect significant patterns related to specialization

Appendix 2

Exhibit 3.3: PRFs - Cor	nmercial Lines						
		Inci	uding Minor L	lines	Excl	uding Minor	Lines
Line of Business (LOB)		Specialists	Non- Specialists	Difference	Specialists	Non- Specialists	Difference
A	Homeowners/Farmowners	0.973	0.963	0.01	0.918	0.957	-0.039
В	Priv. Passenger Auto Liability	1.015	0.98	0.035	0.993	0.972	0.02
c	Commercial Auto Liability	1.029	0.98	0.05	0.997	0.979	0.018
D	Workers' Compensation	1.083	1.052	0.031	1.059	1.037	0.022
E	Commercial Multiperil	1.012	0.917	0.094	0.911	0.878	0.033
G	Special Liability	0.97	1.019	-0.05	0.848	0.976	-0.128
н	Other Liability	0.996	1.026	-0.03	0.974	1.039	-0.065
1	Special Property	0.843	0.834	0.008	0.804	0.82	-0.016
J	Auto Physical Damage	0.876	0.863	0.013	0.816	0.844	-0.028
к	Fidelity & Surety	0.848	0.811	0.036	0.732	0.6	0.132
L	Other	0.943	1.007	-0.065	0.897	0.956	-0.059
0	Reinsurance B	1.59	1.504	0.085	1.462	1.319	0.143
R	Products Liability	1.22	1.267	0.048	1.134	1.277	-0.143





Diversification Credit

- Divide companies by size (5 bands) and diversification ranking (6 bands, including one band for monoline = 0 diversification)
- Calculate 87.5th percentile PRF for all lines combined within each diversification/size cell
- If no diversification effect, PRFs constant down columns
- Decrease in PRF down a column is measure of diversification benefit



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Appendix 3

All Lines Diversification: Findings

Appendix 3

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- Rather than a simple pattern we find several regions
 - Benefit for diversification increases down column for smallest sizes
 - Benefit for diversification from diversification band 0 to band 2 for larger companies
 - Little apparent benefit of diversification for larger three size bands beyond diversification band 2

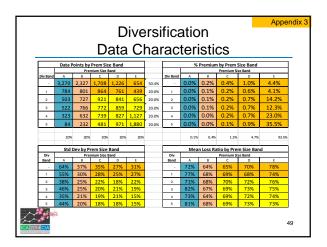
Indicated -NAIC Diversification						
Div		Pre	mium Size E	and		
Band	А	В	с	D	E	
0	45%	25%	24%	26%	35%	
1	47%	20%	26%	22%	40%	
2	42%	21%	16%	18%	15%	
3	44%	21%	20%	19%	19%	
4	35%	14%	20%	20%	18%	
5	52%	24%	15%	18%	17%	
Data			17.8%			

Diversification Data Characteristics

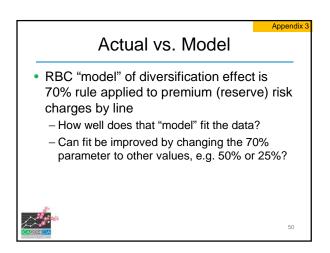
- Number of data points uniformly distributed, as intended
- Most premium is in "lower right corner"
- Standard deviations behaves somewhat as expected
- Loss ratios vary by size/diversification data cell
- Loss ratio, standard deviation and distribution by cell drive 87.5th percentile

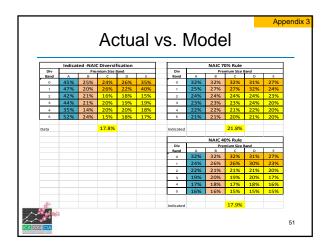


Appendix 3

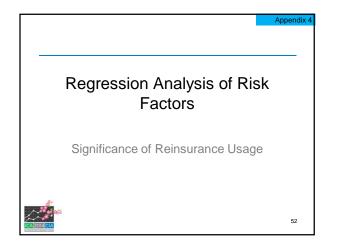






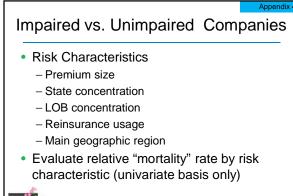




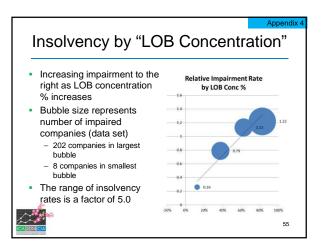


Insolvency History

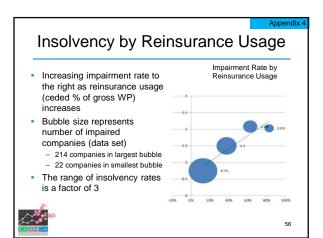
- 397 impaired companies
- 3,287 unimpaired companies
- 10.8% impairment over 14 years
- 0.8% impairment rate per year
 - This count may not be complete
 - Our main objective is to review risk characteristics of insolvencies; for that purpose a representative sample is sufficient



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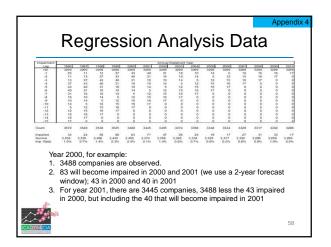
Regression Analysis Model

The two-year impairment probability for the i^{th} company, p_i , is assumed to be a logistic function of n predictive variables

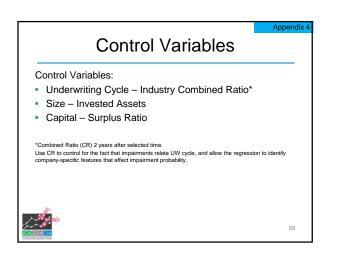
 (X_n) : Logit(p_i)=B0+ B1 X_{1i} + B2 X_{2i} +...+ Bj X_{ni},

where, $Logit(p_i)=In(p_i /(1-p_i))$.

The explanatory variables can be either continuous or categorical.



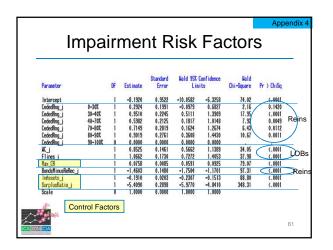




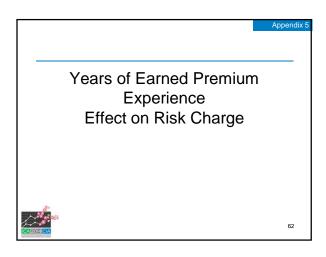
Significant Risk Factors

Company Risk Factors

- Reinsurance recoverable (on paid loss) portion of assets (higher is bad)
- Ceded Reinsurance (complicated pattern)
- LOB Risks: WCA or Financial LOB concentration
 - Perhaps a feature specific to 1996-2010 analysis period
 - Another feature that may be specific to the time period is that Medical Professional Liability shows lower than average risk in 1996-2010 period



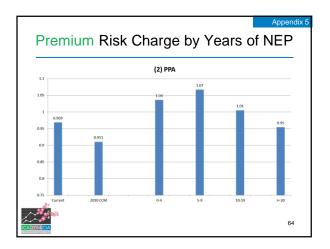




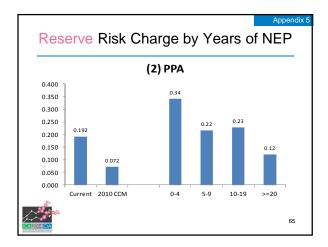
Mature Companies = Lower Risk

- Baseline excludes data points from companies with less than five years of non-zero net earned premium (NEP)
- Often, but not universally, indicated risk charge declines for business with longer history
- For long tail lines, the effect of "development maturity" may be confounded by the effect of "longer history", making "older age" look less important than it is

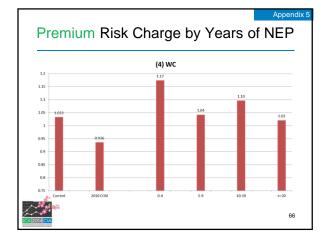




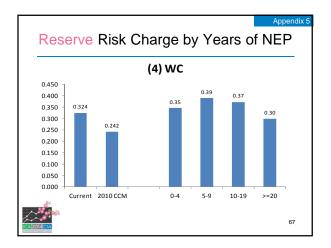




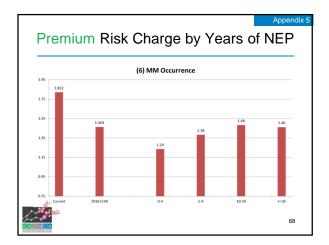




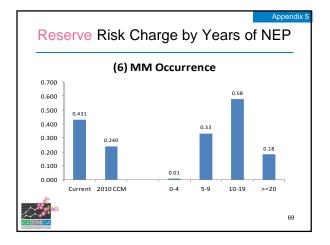




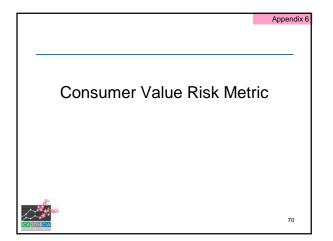


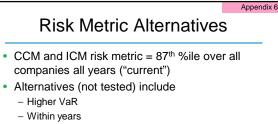












- Within companies
- TVaR or other risk metric
- Alternative treatments of UW cycle
- "Consumer Value" measure

Consumer Value Parameters

Rather than "arbitrary" VaR or TvaR selections, "Consumer Value" parameters are

- · Cost of Capital
- Consumer Utility Function (what is certainty equivalent of losses of various size)
- Distribution of insurer's potential total losses



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Appendix 6

"Consumer Value Risk Metric"

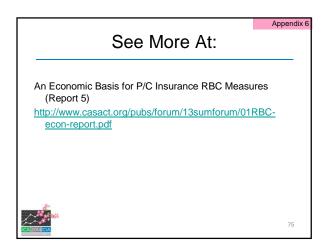
Appendix 6

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- Optimize "consumer" value considering:
 - Benefit of lower default risk from capital increase
 - Cost of higher premium from capital increase
- Optimized risk metric is VaR of loss distribution transformed to give higher probability weight to losses in the tail
- Shape of consumer value is not highly sensitive to capital near the optimum level



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DCWP: The People The Work Product

Deverview of Dependencies and Calibration in the RBC Formula (Report 1) www.casact.org/pubs/forum/12wforum/DCWP_Report.pdf 2011 Research – Short Term Project (Report 2) www.casact.org/pubs/forum/12wforum/RBC_URWP_Report.pdf Solvency II Standard Formula and NAIC RBC (Report 3) http://www.casact.org/pubs/forum/12fforumpt2/RBC-DCWPRpt3.pdf A Review of Historical Insurance Company Impairments (Report 4) http://www.casact.org/pubs/forum/12fforumpt2/RBC-DCWPRpt4.pdf

Appendit

В

DCWP Reports in Preparation

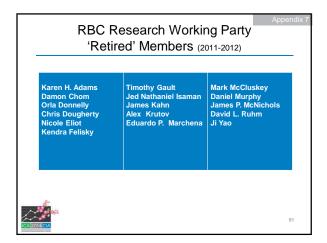
- Application of Solvency II Calibration Method to RBC Premium and Risk Factors
- Regression analysis of risk factors associated with insurance company impairments
- Reserve Risk Factors Individual Company Basis vs. NAIC RBC Basis
- Dependency and Credit for Diversification in NAIC RBC Formula
- Risk Metric Time Horizon Analysis (extension of Report 5)
- Impact Analysis Assessment of effect of changes in RBC Formula by type of company

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 RBC Premium Risk Factor Calibration based on Combined Ratio Rather than Loss Ratio









Work Stream Leaders						
Work Stream	Leader	Team				
Overview Reports 1 and 2	Rept-1 A. Kaufman Rept-2 D. Murphy	Committee members as listed on those reports				
3. Solvency II Formula and RBC	Joe Cofield	Christina Zhou				
4. Insolvency Risk Factors-Univariate	Ed Marchena					
5. Risk Metric	Bob Butsic	Sholom Feldblum, Glen Meyers				
6. Premium Risk Factors	Jennifer Wu, Dennis Franciskovich	Karen Adams, Franco LePera, Daniel Murphy, Tim Sweetser				
7. Reserve Risk Factors	Jennifer Wu	Karen Adams, Dennis Franciskovich, Franco LePera, Daniel Murphy, Tim Sweetser				

Work Stream	Leader	Team
8. Risk Charge by Type of Company	Ashley Reller	
9. Solvency II Calibration	Jeff Pflugger, Tim Sweetser	Glen Meyers
10. Insolvency risk Factors- Regression	Jose Couret	
11. Rsv Risk Charge - Individual Co Model vs. RBC	Manolis Bardis	Christian Citarella, Glen Meyers, Linda Zhang, Damon Chom
12. Dependency	Apundeep Lamba	Shiwen Jiang, Glen Meyers, Dan Murphy, Damon Chom
13. Impact Analysis	Ron Wilkinson	Ji Yao, Damon Chom, Dean Guo
14. Combined Ratio	Douglas Nation	

