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# "Undertaking Specific Parameters or a Partial Internal Model under Solvency 2?"

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# Agenda



- Introduction
- USPs within Non-Life Premium Risk
- Towards a Partial Internal Model for Premium Risk
- GLM, GAM or Mixture of them?
- Case study: USPs versus PIRM
- How about volatility?
- Conclusions
- References

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### Introduction



Solvency 2 directive represents a complex project for  $\overline{reforming}$  the present vigilance system of solvency for European insurance companies.

### ■ W/bat?

A definition of a **Solvency Capital Requirement** ("SCR") as an economic capital to reflects the **true risk profile** of the undertaking, taking account of **all quantifiable risks**, as well as the net impact of **risk mitigation techniques**.

# Distribution of Total Losses Expected Losses VaR<sub>99,5</sub> O.5% Total Losses

### SCR

- Time Horizon: 1 year
- Risk Measure: Value at Risk
- Probability of Ruin: 0.5%

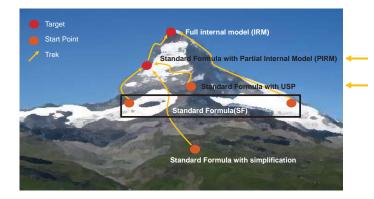
PIRM under Solvency 2?

### Introduction



• How?

In principle, Solvency 2 provides a range of methods to calculate the SCR which allows undertakings to choose a method that is **proportionate to the nature**, **scale and complexity of the risk** that are measured.



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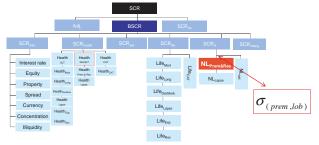
# Introduction



The scope of this work is to compare the USPs' methodologies proposed in QIS5 with a PIRM for **premium risk**.

In particular we introduce this approach:

- for Personal Line insurance and/or for each product priced using regression techniques
- in order to stress the value of the model used from Pricing Staff



The premium risk is defined in the TS of QIS5: [2] "Premium risk results from fluctuations in the timing, frequency and severity of insured events (...). Premium risk includes the risk that premium provisions turn out to be insufficient to compensate claims or need to be increased. Premium risk also includes the risk resulting from the volatility of expense payments.(...)".

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## USPs within Non-Life Premium Risk



$$\sigma_{(\mathit{prem}\,,\mathit{LoB}\,)} = c \cdot (\sigma_{(\mathit{U}\,,\mathit{prem}\,,\mathit{LoB}\,)}) + (1 - c) \cdot \sigma_{(\mathit{M}\,,\mathit{prem}\,,\mathit{LoB}\,)}$$

Undertakings can replace a part of standard parameters with specific parameters (USP):

 According a criterion of credibility that depends on LoB and the length of the time series Nlob used for the estimation:

For GTPL, MTPL, Credit and Suretyship:

$N_{lob}$	- 5	6	7	8	9 67%	10	11	12	13	14	≥15
C	34%	43%	51%	59%	67%	74%	81%	87%	92%	96%	100

For the other LoBs:

	$N_{lob}$	5	6	7	8	9	≥10
1	C	34%	51%	67%	81%	92%	100%

 The data used for the calculation of undertaking-specific parameters should be complete, accurate and appropriate.

## Which USPs to choose?



	Method 1	Method 2	Method 3
Assumptions	The expected loss is proportional to the premium The company has a different but constant expected loss ratio ("ELR")  The least squares fitting approach is appropriate	In addition to the assumptions of Method 1:  • The distribution of the loss is lognormal  • The maximum likelihood fitting approach is appropriate	A separate analysis of the random variables number of claims and cost per claims     Based on the Swiss Solvency Test approach (Gisler, 2009)
Approach	This method use the Ultimate Cost after one year by accident year The Volatility depends on volatility year by year of Earned Premium or ELR One year of adverse claim experience can produce material effects on the volatility The company tends to reserve prudently in the first accident year	It is a method similar to the previous	The approach is significantly influenced by the variability in the exposure and in the number of claims Requiring a greater number of information than the other two methods If the company has reserved less prudently in the first development year, probably it has a volatility higher than the values obtained with Methods 1 and 2.

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# Towards a Partial Internal Model for Premium Risk



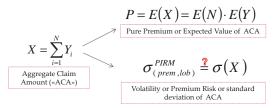
• Why?

With a (Partial) Internal Risk Model, an Insurance Company can calibrate the volatility of its business and risk profiles.

$$\boxed{\sigma_{(prem,lob)}^{SF}} \geq \boxed{\sigma_{(prem,lob)} = c \cdot \sigma_{(U,prem,lob)} + (1-c) \cdot \sigma_{(M,prem,lob)}^{SF}} \geq \boxed{\sigma_{(prem,lob)}^{PIRM}}$$

### **Premium Risk**

Undertakings, therefore, will have to evaluate the **error in the assumptions**, **models or methods** used to **solve** a **pricing problems**.



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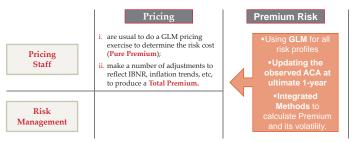
# Different prospective



The **new idea** of this presentation is represented by:

$$\sigma_{(prem,lob)}^{PIRM} = \sigma(X)$$

This seems to be in contrast with the definition of SCR, but in a PIRM: "Insurance and reinsurance undertakings may use a different time period or risk measure (...) to calculate the Solvency Capital Requirement in a manner that provides policy holders and beneficiaries with a level of protection equivalent to that set out in Article 101" (art. 122(1) S2 directive)



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# GLM, GAM or a Mixture of these? GLM is a benchmark within this technical framework: • How to manage continuous rating variables? • Is Cluster Analysis a good solution? • An obvious disadvantage is that the premium for two policies with different but close values for the rating variable may have substantially different premiums if the values happen to belong to different intervals This is what we propose: Mixture Data Analysis Cluster Analysis Cluster Analysis Cluster Analysis Analysis Cluster Analysis Analysis Cluster Analysis Analysis

# Case study: USPs versus PIRM



### **Perimeter**

Hypothetical portfolio - Car

- Size: Medium (in term of Volume)
- Lob: Motor Third Party Liability solo
- Nlob: 15 years
- Insurance Portfolio: all risks which are associated claims and any (ultimate 1-year) costs incurred by year (2009-2011).

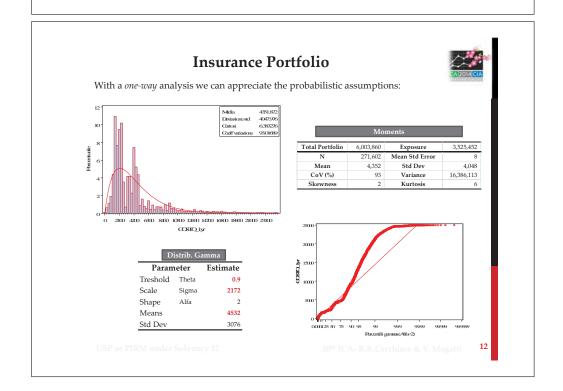
### **Purposes**

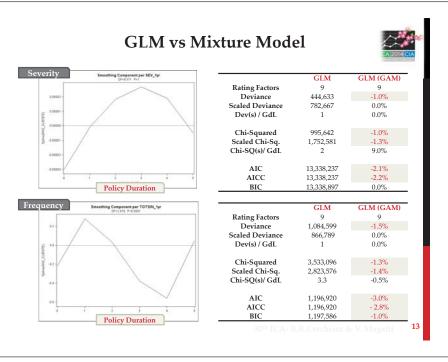
- Estimating the impact of the use of USPs
- Defining the «Best Model» with goodness of fit analysis between a GLM or GLM after a GAM analysis («Mixture Model», «GLM(GAM)»)
- A comparison between the SF market parameters, USPs and the standard deviation of the model

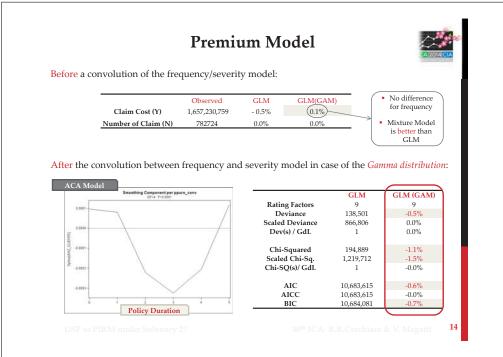
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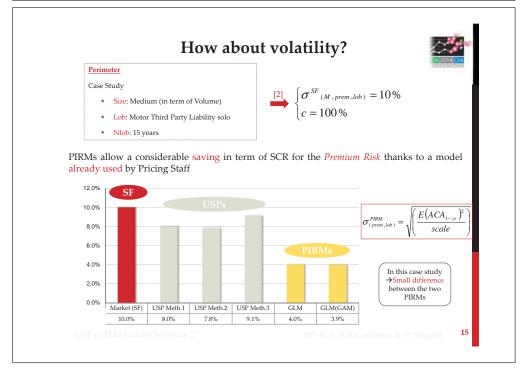
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### **Conclusions**



	Standard Formula	USPs	PIRM
Pro	Factor based or scenario based     Quite simple to deploy	Risk based on the historical data     The volatility could be lower than SF	■ Strength connection → Pricing/Premium Risk ■ The volatility could be lower than USPs
Contro	It can't take into account the risk mitigation techniques	Data: complete, accurate and appropriate     Great demand for documentation	In addition to USPs:  • More detailed Preapplication process to approve it;

### Future Developments - PIRM

- Determine the 99.5% percentile of the ACA distribution
- Explore other statistical models to evaluate the random effects (e.g. GEE and GLMM)
- Evaluate different models for Attritional Losses and Large Losses (e.g. GLM within a Quasi-Likelihood approach)
- Use an (Ultimate 1-year) Aggregate Claim Amount net of the reinsurance
- Check the model for a total MTPL business (car, motorcycle, moped, etc.)
- Define a way to aggregate different LoBs and discover the correlation with Reserve/CAT risk

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### Thank you