

# Reserving for Life Insurance in a Low Interest Rate Environment – Additional Interest Provisions

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Allianz Lebensversicherungs-AG

# About the speaker

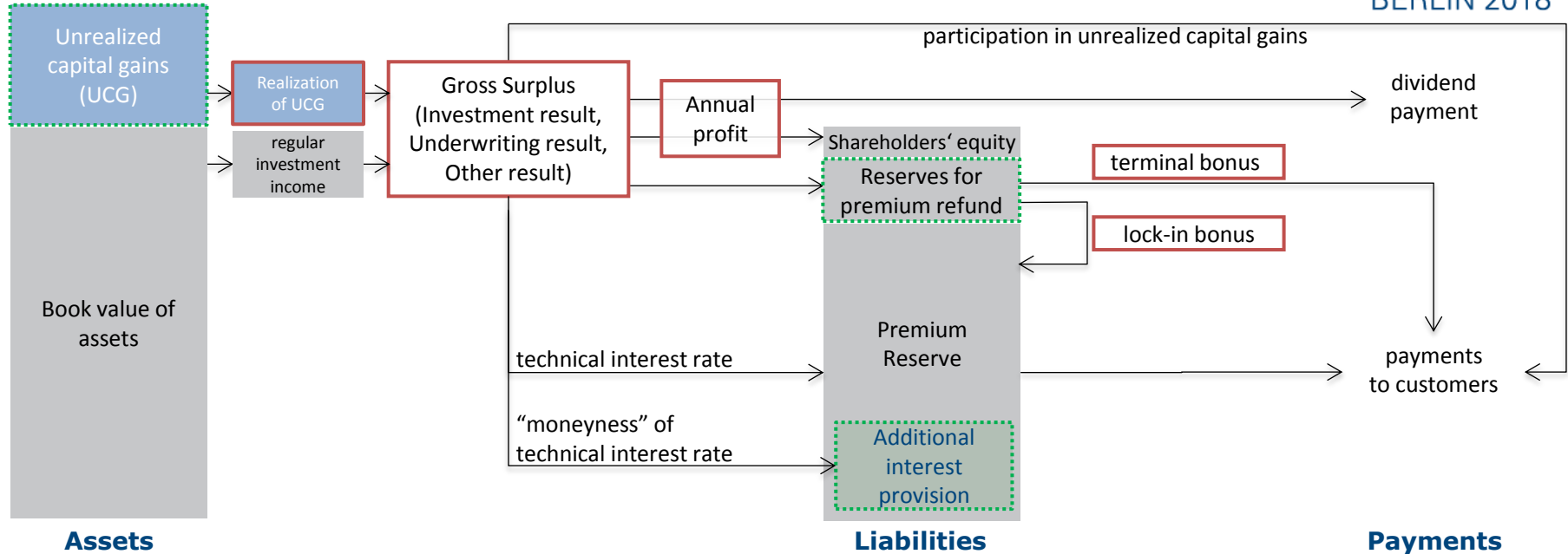


- **Dr. Wolfgang Siegert**
- Member of actuarial research unit at Allianz Lebensversicherungs-AG since 2009
- Member of the German Actuarial Association (DAV) since 2012
- In 2007 joined Allianz Lebensversicherungs-AG (2007-2009: product development);
- Studies in Mathematics, focusing on Stochastic Analysis:
  - Ph.D. from Humboldt University Berlin (2007),
  - Diploma degree from Regensburg University (2003),
  - academic year 2000/2001 at Brandeis University (USA).

Allianz 

- **Allianz Lebensversicherungs-AG**
- German Life entity of Allianz SE
- Market leader in Germany, market share of 20,4% in 2016

# Reserves in German life insurance (sketch)

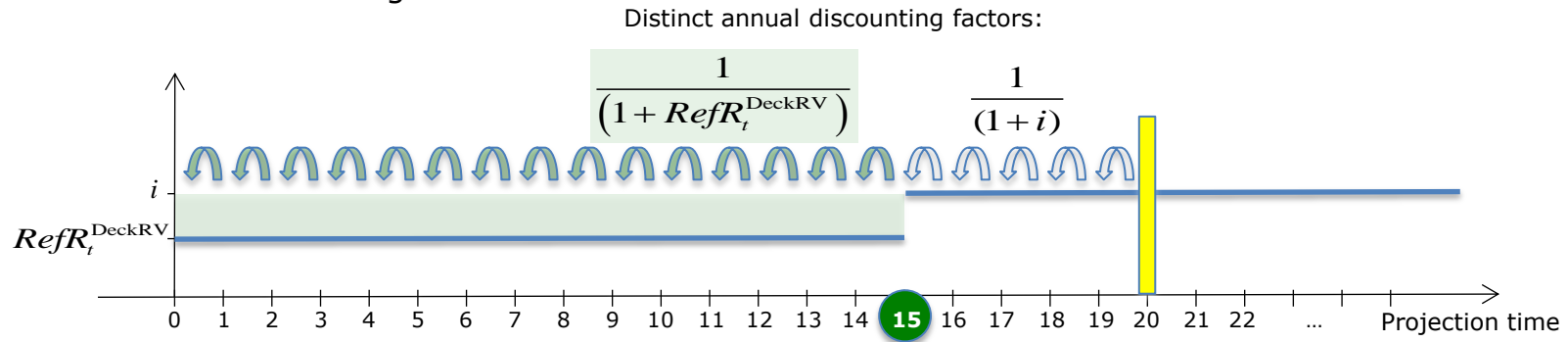


... buffer    ... subject to steering

# Additional interest provision in Germany (ZZR)

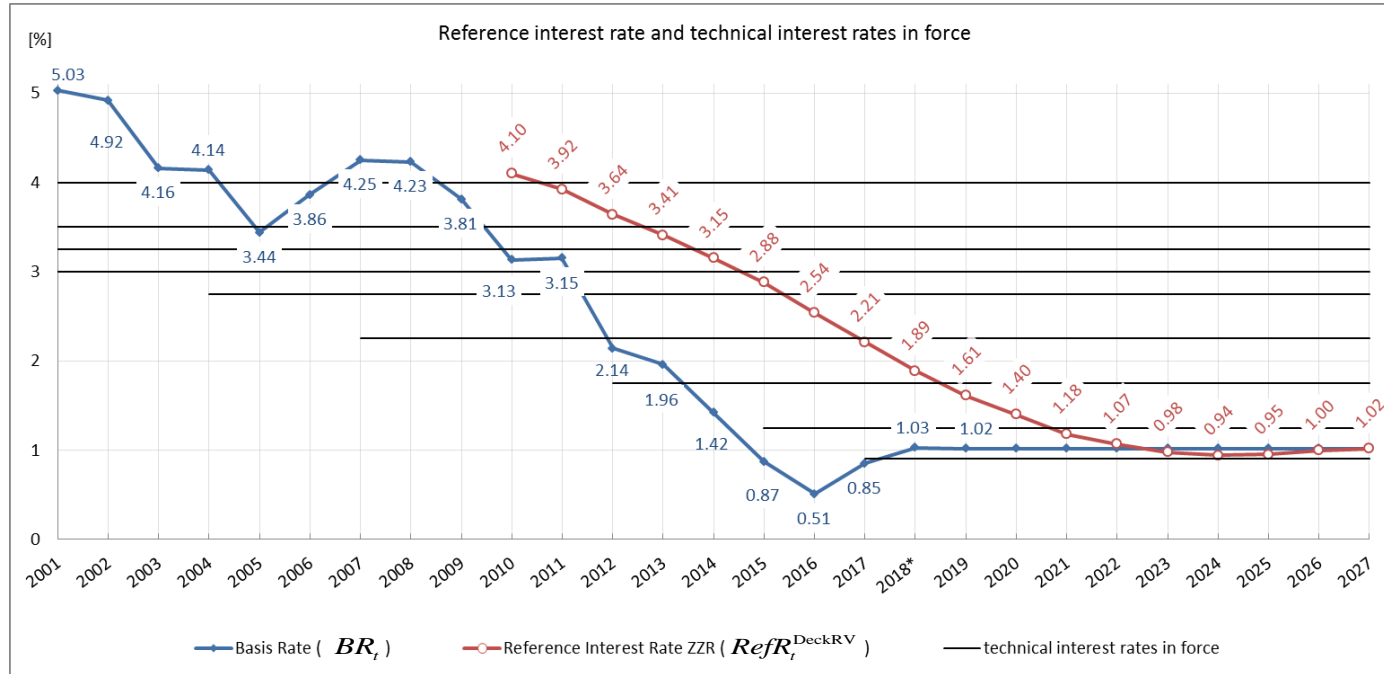
Premium reserve for year  $t$  if **expected future earnings** fall short of **interest rate obligations**

- Expected future earnings represented by **reference interest rate**  $RefR_t^{DeckRV}$ :  
10y-mean of **basis rates**  $BR_s$  (annual average of 10y zero-coupon rates).
- Interest rate obligation of given contract represented by its technical interest rate  $i$ .
- Vector of rates used for discounting:



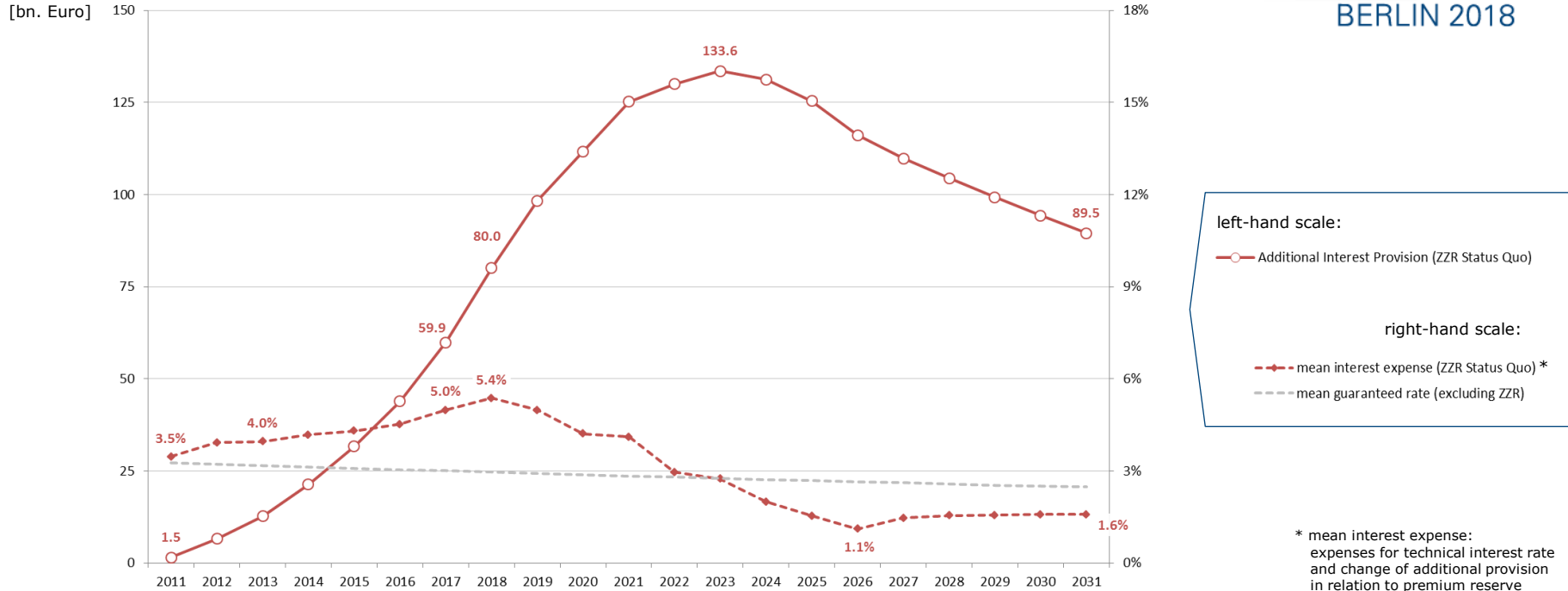
- **Additional interest provision (ZZR):** Part of premium reserve induced by

# Development of reference interest rate (DeckRV): Unanticipated decrease of basis rate after 2011



\* Years 2018 ff.: Extrapolation based on the assumption that the 10y interest rate as of April 30th 2018 persists (1.011%).

# Additional reserve stabilizes German life business - at the expense of unrealized capital gains



Sources: ○: GDV 2018; -♦- and - - -: Own approximations jointly with Michael Dahmen (HDI).

# Additional reserve needs recalibration

Working group<sup>1</sup> of the German Actuarial Association (DAV):

- Long-term reference rate is not to be altered.
  - Pace at which additional reserve ZZR moves needs to be adjusted.
- ⇒ Proposal for new conceptual design of the Additional interest reserve „**Corridor Method**“ (CM):

**CM 1** Corridor dampens movements (increase) of ZZR

**CM 2** Reference rate cannot decrease if exceeded by current basis rate and vice versa

<sup>1</sup> Members: Dr. Uwe Schrader [head], Werner Faigle, Dr. Maximilian Happacher, Gerd-Michael Hartmann, Dr. Johannes Lörper, Dr. Normann Pankratz, Dr. Michael Pannenberg, Carsten Pröhl, Dr. Michael Renz, Dr. Hans Schlierf, Dr. Bodo Schmithals, Dr. Marco Schnurr, Klaus Trautmann, Josef Wagner

*„Es ist weder erforderlich noch ratsam, die Zinszusatzreserve weiterhin im bisherigen Tempo aufzubauen.“*

*BaFin-Präsident Felix Hufeld*

*„It is neither necessary nor advisable to continue setting up this – basically very reasonable – reserve in the current pace.“*

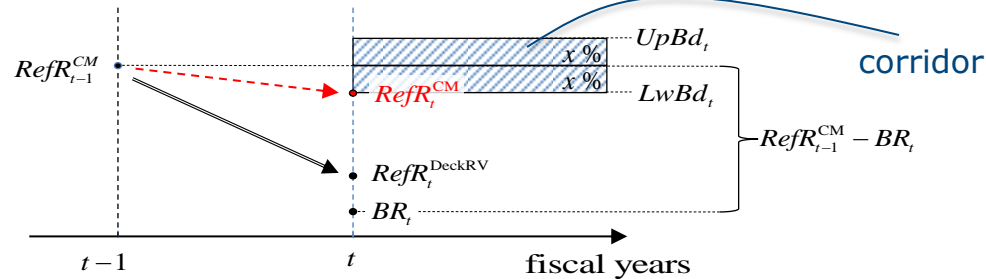
*Felix Hufeld, President of German Federal Financial Supervisory Authority (BaFin).*

# CM 1 Corridor dampens movements (increase) of ZZR

Initial condition:  $RefR_t^{CM} := RefR_t^{DeckRV}$  for fiscal year  $\tau$  (e.g.  $\tau := 2017$ ). For  $t > \tau$ , recursively:

$$UpBd_t := RefR_{t-1}^{CM} + x\% \cdot |RefR_{t-1}^{CM} - BR_t| \quad (\text{upper bound of corridor})$$

$$LwBd_t := RefR_{t-1}^{CM} - x\% \cdot |RefR_{t-1}^{CM} - BR_t| \quad (\text{lower bound of corridor})$$



(depiction for decreasing rates; increasing rates analogously)

- ▷ Substituting  $RefR_t^{DeckRV}$  by  $RefR_t^{CM}$  as the decisive reference interest rate dampens the movement of the additional interest provision (ZZR)

Reminder of notation:

- $RefR_t^{DeckRV}$   
reference interest rate for fiscal year  $t$  according to current regulation
- $BR_t$   
arithmetic mean of interest rates Jan.-Sept. in fiscal year  $t$  (Basis Rate)

Sources: Schrader 2015, Pannenberg / Dahmen / Tiemann 2016

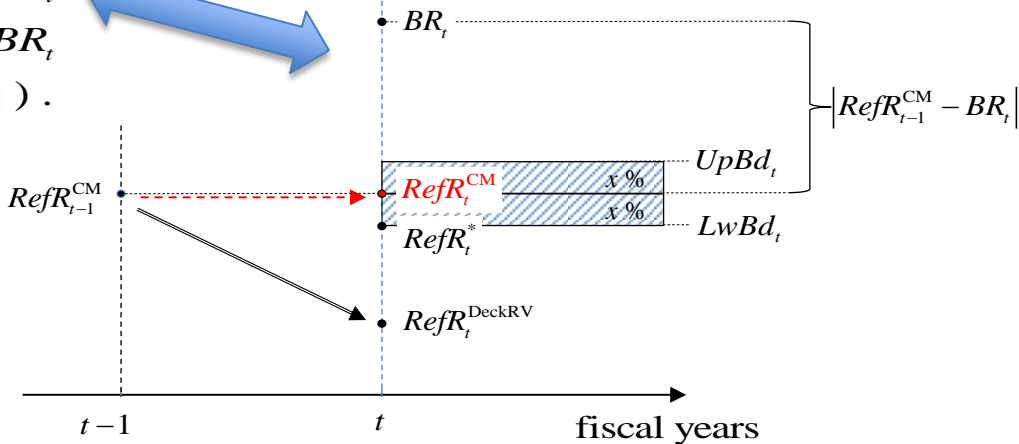
**CM 2**

# Reference rate cannot decrease if exceeded by current basis rate and vice versa



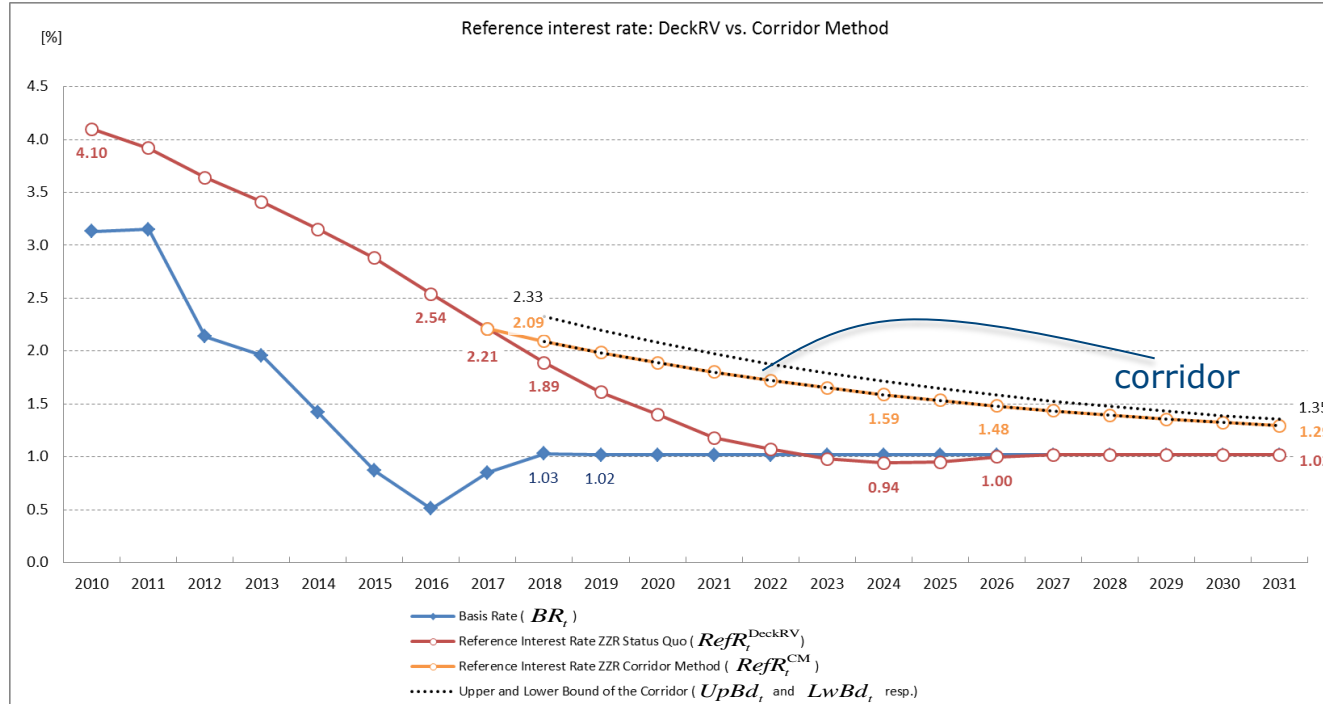
$$RefR_t^* := \begin{cases} UpBd_t & , \text{ if } UpBd_t < RefR_t^{DeckRV} \\ RefR_t^{DeckRV} & , \text{ if } LwBd_t \leq RefR_t^{DeckRV} \leq UpBd_t \\ LwBd_t & , \text{ if } RefR_t^{DeckRV} < LwBd_t \end{cases} = \min \left[ \max \left( RefR_t^{DeckRV} ; LwBd_t \right) ; UpBd_t \right]$$

$$RefR_t^{CM} := \begin{cases} RefR_{t-1}^{CM} & , \text{ if } RefR_t^* < RefR_{t-1}^{CM} < BR_t \\ & \text{ or } RefR_t^* > RefR_{t-1}^{CM} > BR_t \\ RefR_t^* & , \text{ otherwise (see CM 1) .} \end{cases}$$



Sources: Schrader 2015 (did not mention second exceptional case yet), Pannenberg / Dahmen / Tiemann 2016

# CM: Possible scenario of interest rates



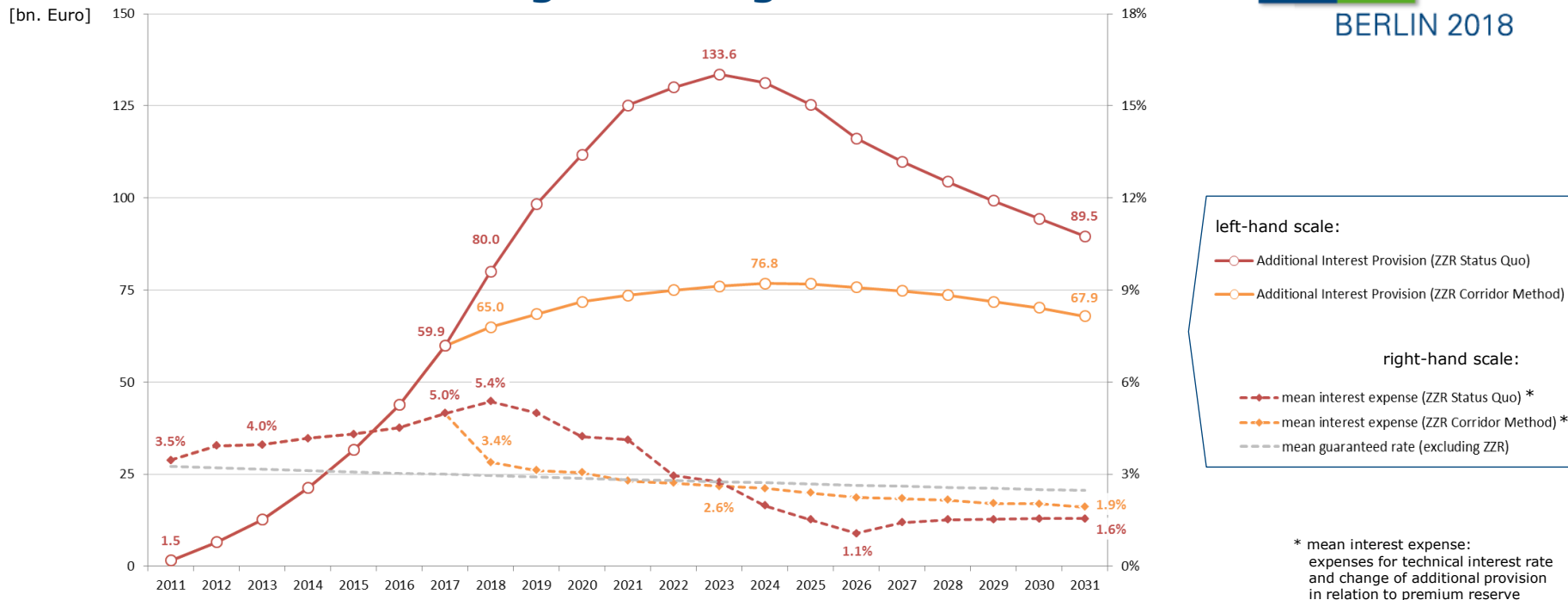
## Assumptions:

- CM enacted in 2018 ( $\rightarrow \tau = 2017$ ).
- 10y interest rate as of April 30th 2018 persists (1.011%)
- $x := 10$

e.g. upper and lower bound in 2018:

$$2.21\% \pm 10\% \cdot |2.21\% - 1.03\%|$$

# CM can save resources for possible surplus participation of recent business adding to inter-generation fairness



Sources: ○ and ○ : GDV 2018; - - - , - - - and - - - : Own approximations jointly with Michael Dahmen (HDI).

# What this talk has omitted



- Austria
- Belgium (knipperlichten)
- Historic development in Germany before 2011
- Additional Interest Provision and the German Regulation on the Minimum Surplus Participation („MindZV“)
- Considerations on lapses, lump sum option by policyholders, costs
- Valuation reserves vs. customers' participation in unrealized capital gains („Sicherungsbedarf“)
- ...

# Summary



- Additional Interest Provision is a valuable tool for stabilizing the German life insurance business in the low interest rate environment
- It needs recalibration to smooth the annual burden for the companies (sustainable speed of build-up)
- DAV working group has tackled the downsides of the current mechanism by proposing the alternative Corridor Method
- Corridor Method needs to be enacted into regulation (DeckRV)

# References & Acknowledgments



- Aktuar aktuell [Notes of the German Actuarial Association (DAV)] Nr. 39, September 2017, pp. 6-7: „Im Interesse der Kunden: Zinszusatzreserve muss neu kalibriert werden“ („In the interest of customers: Additional interest provision needs recalibration“).
- G. Bader 2012: „Die Zinszusatzreserve in der deutschen Lebensversicherung“ („The Additional Interest Provision ZZR in German life insurance“), slides, Zurich 2012/11/15
- BaFin-Journal [Notes of the German Federal Financial Supervisory Authority] November 2017 (p.32): „Zinszusatzreserve: Tempo drosseln“ („Additional Interest Provision: Reduce pace“)
- BaFin-Journal [Notes of the German Federal Financial Supervisory Authority] February 2018 (p.28) on Additional Interest Provision
- J. Bierbaum 2017: „Reservierung langfristiger Garantien“ („Reserving long-term guarantees“), slides, Stuttgart, 2017/11/22
- W. Faigle 2011: „Zinszusatzreserve in der Lebensversicherung“ („The Additional Interest Provision in life insurance“), slides, 2011/04/05
- GDV [Association of German Insurers] 2018: Position Paper („Die Positionen der deutschen Versicherer“), April 2018
- A. Neumann 2013: Allianz Capital Markets Day (Part D on life insurance), 2013/06/25
- K.-U. Schaumlöffel 2018: „Was bringt 2018 aus der Sicht der Versicherungsaufsicht?“ („What will happen in 2018 from the insurance supervision's point of view?“), slides, Cologne 2018/04/25
- U. Schrader 2015: „Bericht aus der AG ZZR des Ausschusses LV“ („Report form the DAV working group of the DAV life committee on the Additional Interest Provision ZZR“), Slides, DAV Autumn meeting 2015/11/16
- M. Pannenberg / M. Dahmen / K. Tiemann 2016: „ZZR – Zeit Zu Renovieren?!“ („Additional Interest Provision - A tIme to Perform a renovation!?“), slides, Cologne 2016/3/1

Kind support by Michael Dahmen in performing the approximations on pages 6 and 11 is gratefully acknowledged.

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**Thank you very much for your attention!**



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# Backup



# Additional interest provision in Germany

- Technical interest rate: Basically constant over time. → Resulting reserve:  $Res_t^{original}$
- “Moneyness” of technical interest rate:
  - If **Reference interest rate** for fiscal year  $t$  falls short of technical interest rate, resulting gap additionally needs to be taken into account in premium reserve at  $t$ .

- Definition of Reference interest rate: 
$$RefR_t^{DeckRV} := \sum_{s=t-9}^t BR_s / 10 ,$$

where „Basis Rate“  $BR_s := \begin{cases} \text{average of rates Jan. to Sept.}, & s = t \text{ (} t \text{: current fiscal year)} \\ \text{annual avg. (Jan. to Dec.)}, & s < t \text{ (past fiscal years)} \end{cases}$

for underlying rates: 10y term, 0-coupon, Euro swap, end of month, published by German Bundesbank.

- Replace technical interest rate by **vector of rates**

$$\begin{cases} \min \{ \text{technical interest rate} ; RefR_t^{DeckRV} \}, & \text{for projection years 1 to 15} \\ \text{technical interest rate} & \text{for projection years 16,...} \end{cases}$$

→ Resulting premium reserve on balance sheet:  $Res_t^{total}$  ( $\geq Res_t^{original}$  in generic cases)

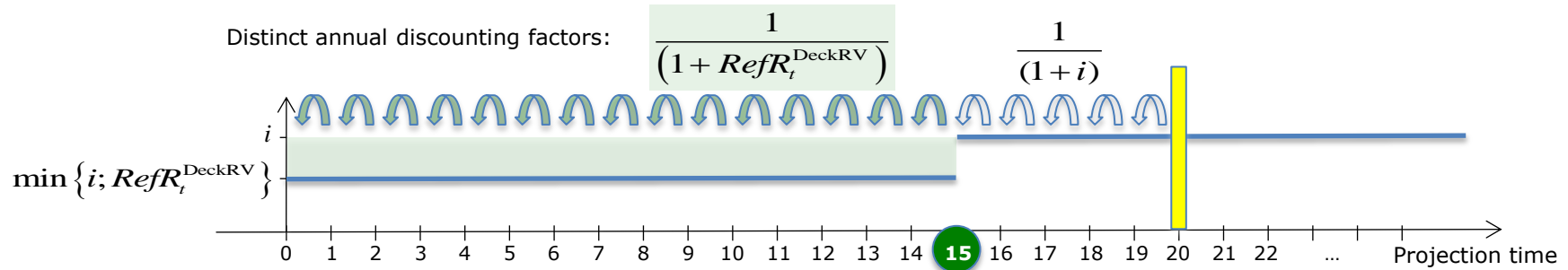
→ **Additional interest provision (“Zinszusatzreserve, ZZR”)**:  $\max \{ 0 ; Res_t^{total} - Res_t^{original} \}$

legal framework: German Commercial Code („HGB“), German Regulation on the Principles Underlying the Calculation of the Premium Reserve („DeckRV“), BaFin circular letter 2016/10/05

# Additional interest provision in Germany (ZZR): Conceptual example

Consider a guaranteed payment of 1 [€] to the customer at time  $T$ , costs etc. ignored.  
Then the following general formula holds:

$$ZZR_t = \underbrace{\frac{1}{(1 + \min \{i; RefR_t^{DeckRV}\})^{\min[T-t; 15]}}}_{\text{total premium reserve on balance sheet}} \cdot \frac{1}{(1 + i)^{\max[0; (T-t)-15]}} - \underbrace{\frac{1}{(1 + i)^{T-t}}}_{\text{"original" reserve}}$$

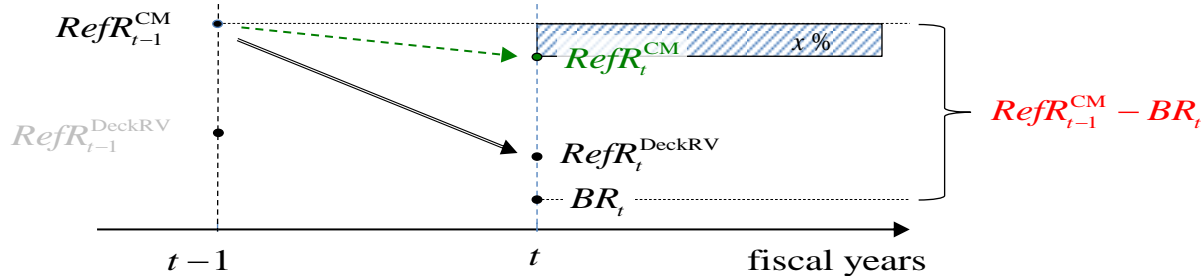


# CM: Equivalent version (case 1)

Initial condition:  $RefR_t^{CM} := RefR_t^{DeckRV}$  for fiscal year  $\tau$  (e.g.  $\tau := 2017$ ). For  $t > \tau$ , recursively:

Case 1: If  $RefR_{t-1}^{CM} > RefR_t^{DeckRV}$ , then

$$RefR_t^{CM} := \max \left\{ RefR_t^{DeckRV} ; RefR_{t-1}^{CM} - x\% \cdot \max(0 ; RefR_{t-1}^{CM} - BR_t) \right\} .$$



▷ In comparison with the absolute value function  $| \dots |$  of the algorithm's previous version, the maximizations in blue color,  $\max(0 ; \dots)$ , now causes **CM 2**.

Reminder of notation:

- $RefR_t^{DeckRV}$   
reference interest rate for fiscal year  $t$  according to current regulation
- $BR_t$   
arithmetic mean of interest rates Jan.-Sept. in fiscal year  $t$  (Basis Rate)

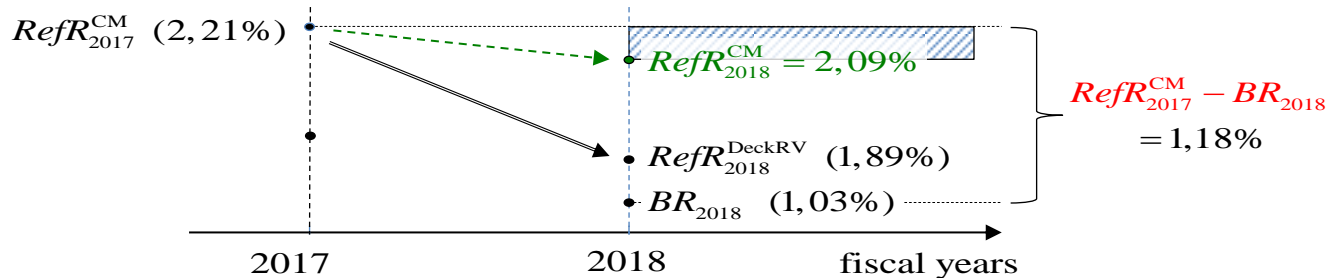
Source: DAV working group

# CM: Equivalent version (example: 2018)

E.g.  $t = 2018$  ( $\rightarrow \tau = t - 1 = 2017$ ).

Assume that interest rates as of April 30th 2018 stay unchanged and  $x := 10$ . Then:

$$2,21\% = RefR_{2017}^{DeckRV} \stackrel{I.C.}{=} RefR_{2017}^{CM} > RefR_{2018}^{DeckRV} = 1,89\% \quad (\Rightarrow \text{Case 1})$$



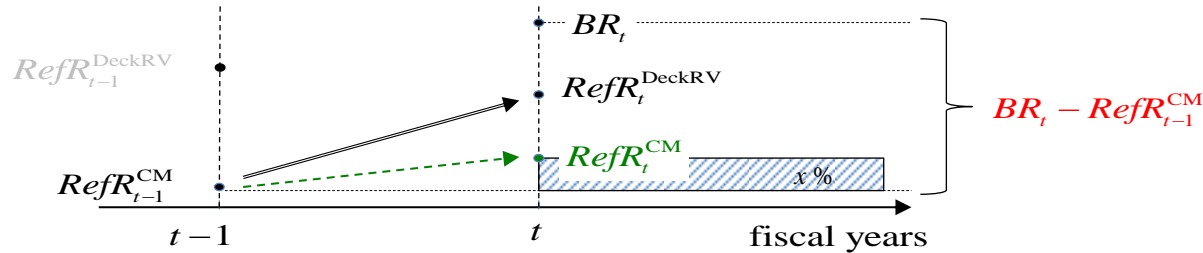
$$RefR_{2018}^{CM} := \max \left\{ 1,89\% ; 2,21\% - \underbrace{10\% \cdot \max(0 ; 2,21\% - 1,03\%)}_{0,118\%} \right\} = 2,09\% . \quad (\text{rounding to 2nd decimal place})$$

# CM: Equivalent version (case 2)

Initial condition:  $RefR_t^{CM} := RefR_t^{DeckRV}$  for fiscal year  $\tau$  (e.g.  $\tau := 2017$ ). For  $t > \tau$ , recursively:

Case 2: If  $RefR_{t-1}^{CM} \leq RefR_{t-1}^{DeckRV}$ , then

$$RefR_t^{CM} := \min \left\{ RefR_t^{DeckRV} ; RefR_{t-1}^{CM} + x\% \cdot \max(0 ; BR_t - RefR_{t-1}^{CM}) \right\},$$



▷ In comparison with the absolute value function  $| \dots |$  of the algorithm's previous version, the maximizations in blue color,  $\max(0 ; \dots)$ , again causes **CM 2**.

Reminder of notation:

- $RefR_t^{DeckRV}$   
reference interest rate for fiscal year  $t$  according to current regulation
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