

# Finnish reference mortality K2004 and mortality trends

IAA Life 2007 in Stockholm

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# Finnish reference mortality K2004

- Cohort model
- No safety margin
- For Finnish life insured
  - Risk selection is based on Retro Life Assurance company's *Guidelines for risk assessments in life and sickness insurance*



# Finnish reference mortality K2004

- Based on
  - Finnish population mortality 1960-2001
  - Finnish life insured mortality 1991-2001
- Has been done with Lee-Carter method with Singular Value Decomposition (SVD)
  - Least-squares fit by using SVD has been made to population data and the result was converted to mortality of life insured

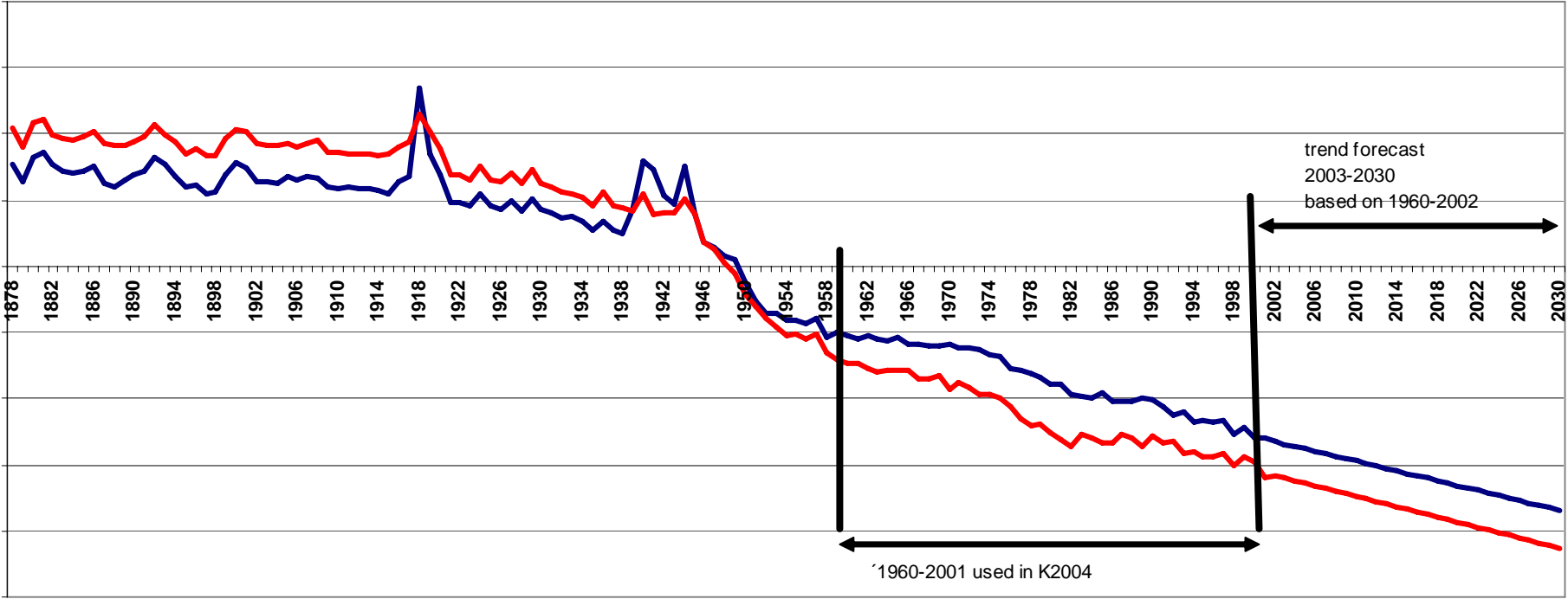


# Singular Value Decomposition (SVD)

- Doing SVD to population mortality results two different matrices, Delta represents yearly change of mortality and Beta describes strength of change in different age groups



Finnish mortality trends 1878-2002 [Delta]



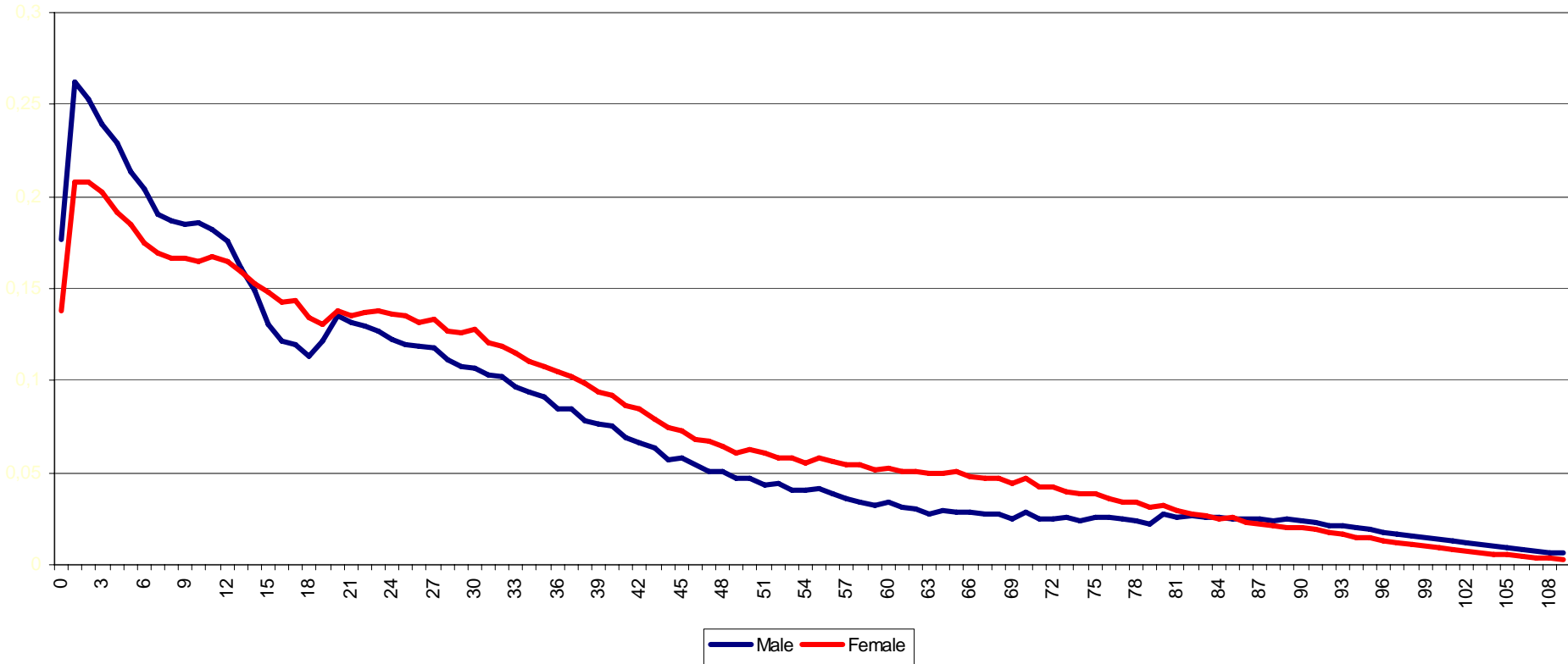
Male Female



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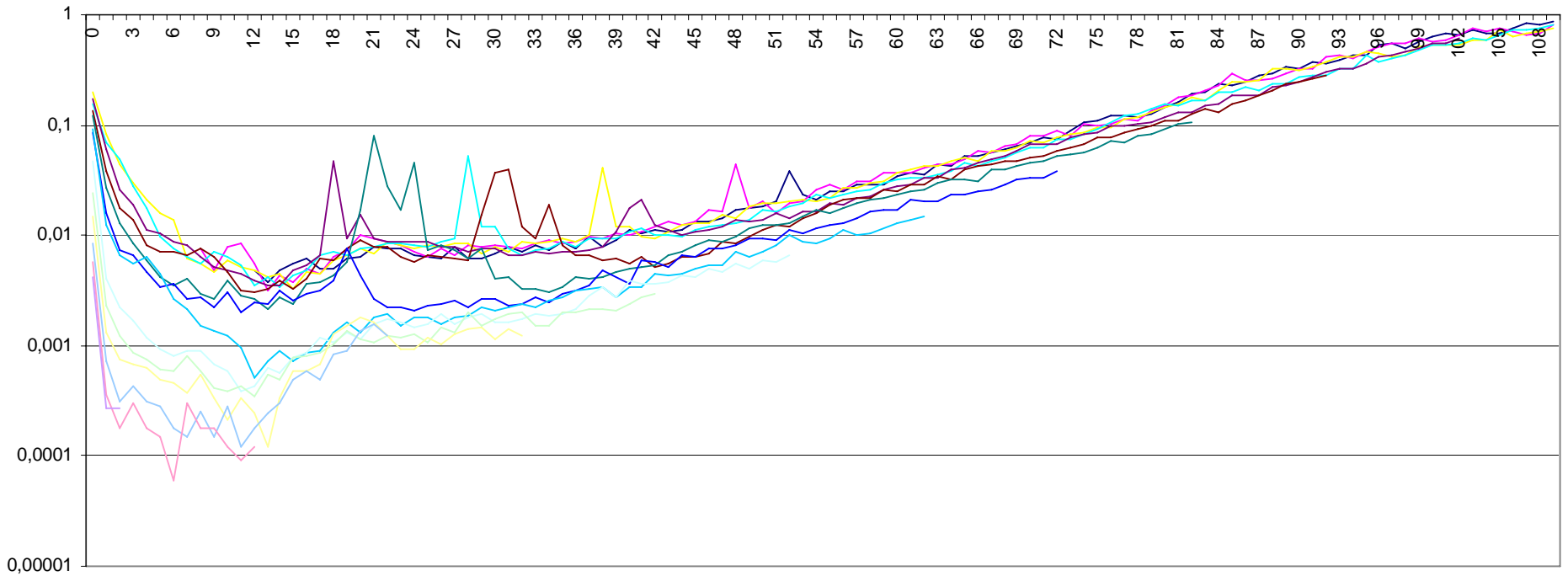
Changes in mortality per age (1878-2002) [Beta]



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Observed mortality cohorts (log scale)  
Males



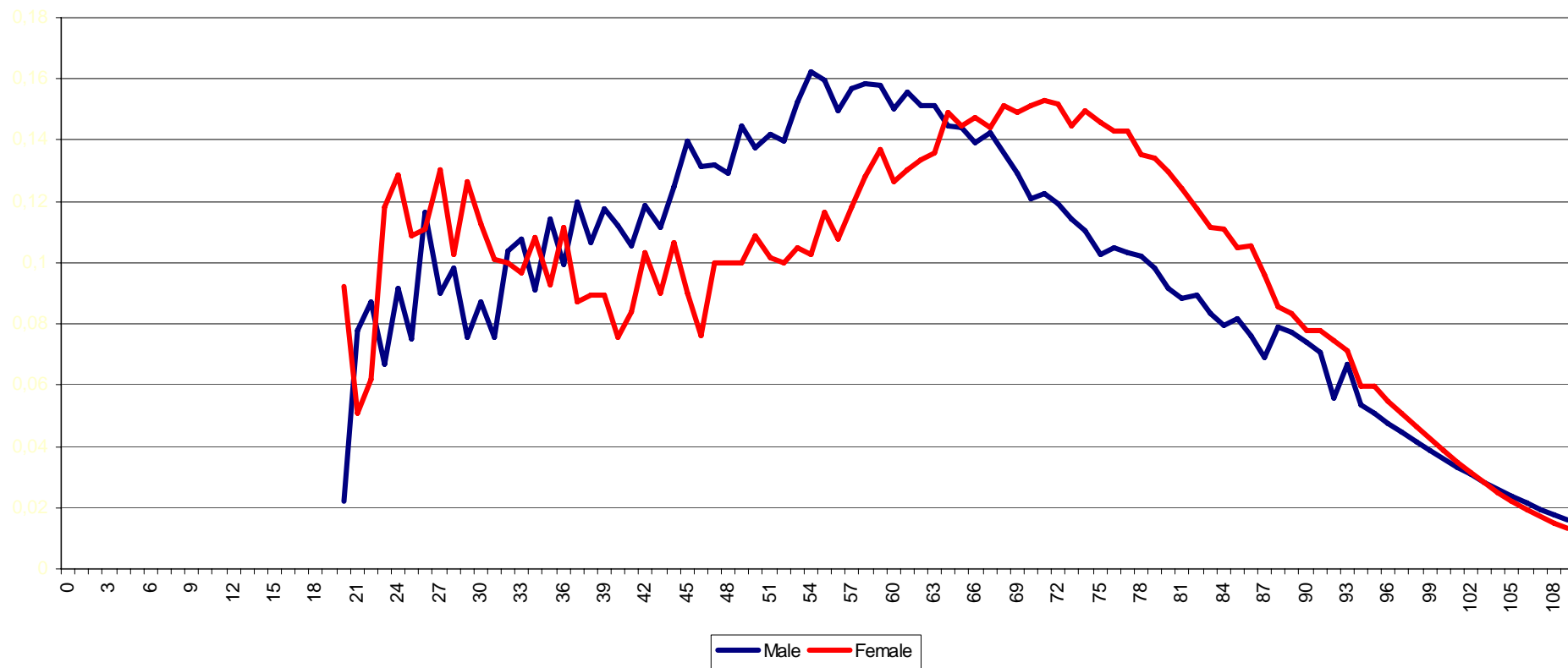
— Born at 1866 — 1870 — 1880 — 1890 — 1900 — 1910 — 1920 — 1930 — 1940 — 1950 — 1960 — 1970 — 1980 — 1990 — 2000 — 2010



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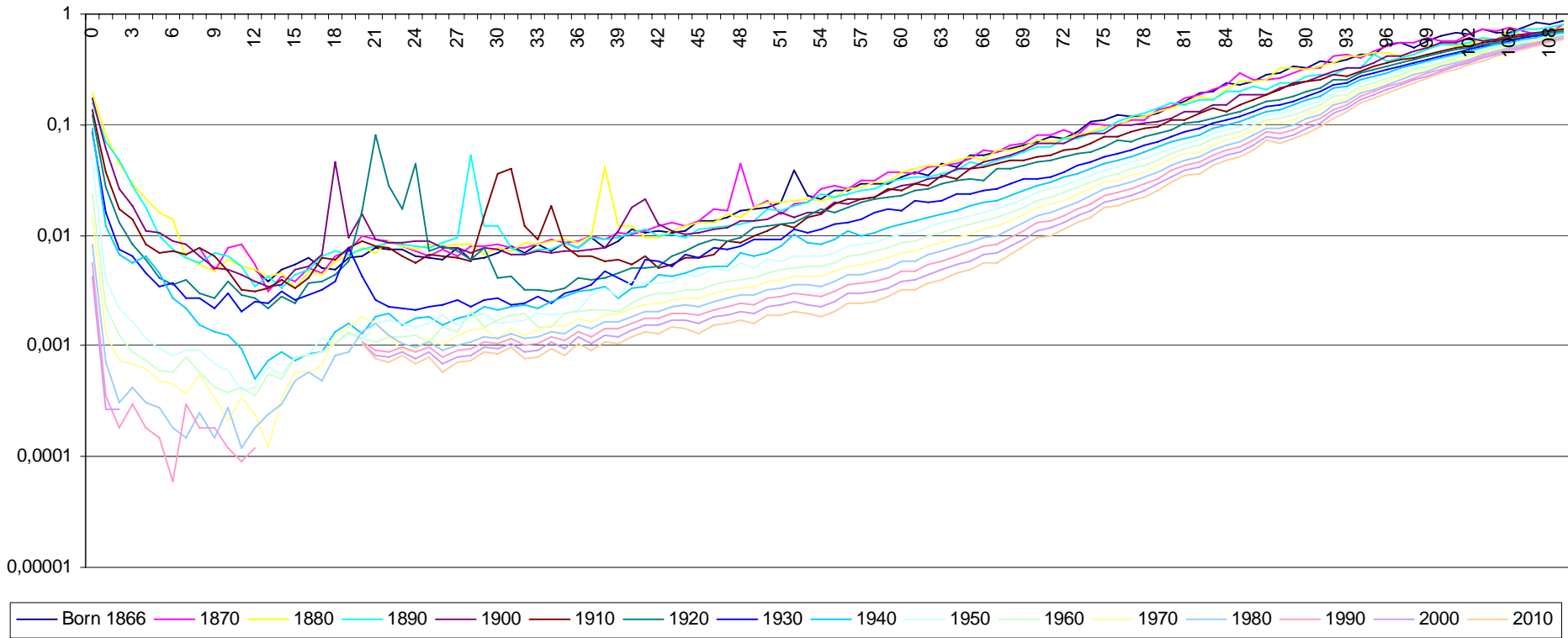
Changes in mortality per ages 19-110 (data 1960-2002) [Delta]



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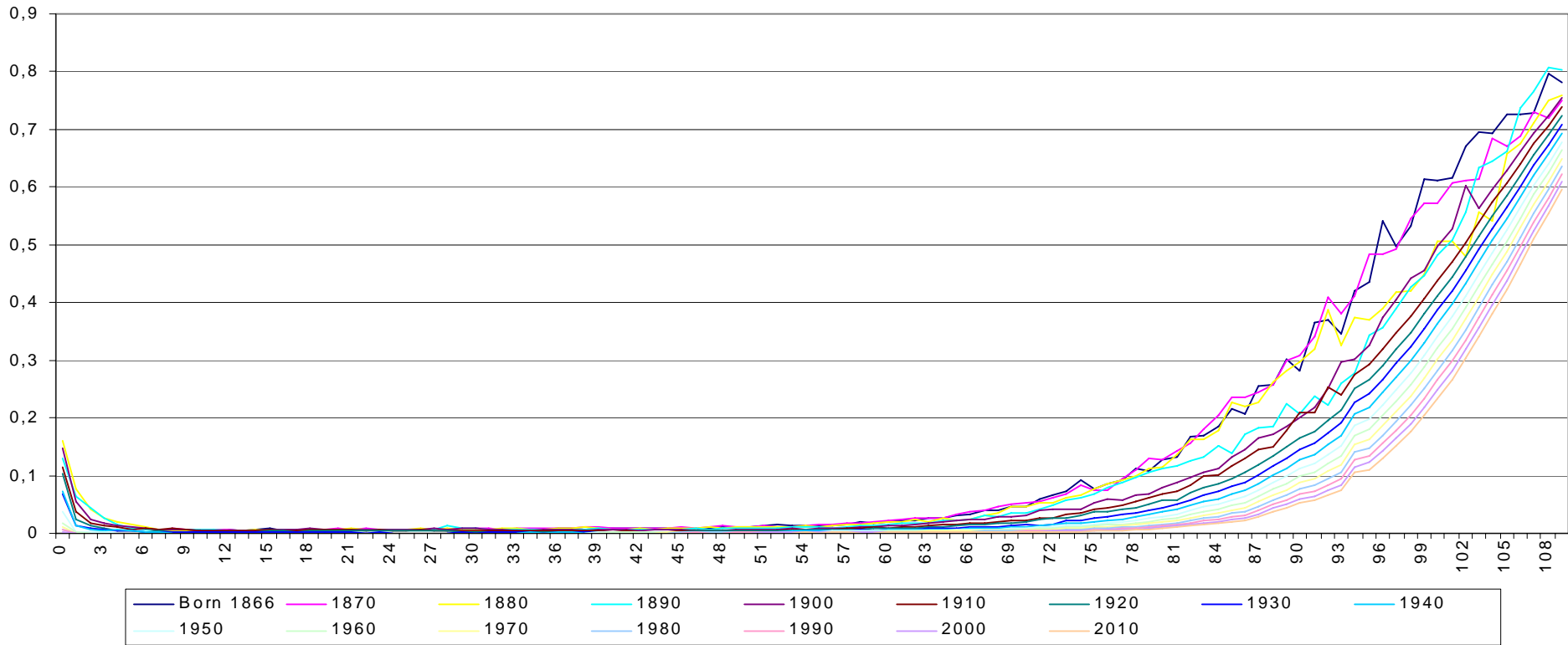
Observed mortality cohorts and forecast (log scale)  
Males



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## Observed mortality cohorts and forecast Females



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# Finnish reference mortality K2004

K2004 mortality for an insured born in year  $sv$  and aged now  $x$  year is:

$$\mu_{sp}(x, sv) = \max\{0.0001, a_{sp}(sv)\} + e^{c_{sp}(x, sv)}$$

where gender-depedent (male  $sp=0$ , female  $sp=1$ ) functions are

$$a_0(sv) = 10^{-5} \cdot 0.744 \cdot (2070 - sv)$$

$$a_1(sv) = 10^{-5} \cdot 0.206 \cdot (2019 - sv)$$

$$c_0(x, sv) = 0.05438 \cdot (1716 - sv) + 0.000533 \cdot (sv - 1719) \cdot x - 0.000217 \cdot (sv - 1843) \cdot \max\{0; x - 81\}$$

$$c_1(x, sv) = -11.51 + 0.000316 \cdot (2253 - sv) \cdot x - 0.000783 \cdot (sv - 1916) \cdot \max\{0; x - 71\}$$



# Future development and possible problems

- How will the trend continue?
- Follow-up of mortality development
- Small Finnish market -> small portfolio of life insured



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